

# Accelerating Configuration Interaction Calculations for Nuclear Structure

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# Eigenvalue Computation by Implicitly Restarted Lanczos

## ► How it works

1. Lanczos factorization:  $HV_{k+p} = V_{k+p}T_{k+p} + fe_{k+p}^T$
2. Implicit restart:  $H(V_{k+p}Q) = (V_{k+p}Q)(Q^T T_{k+p} Q) + fe_{k+p}^T Q$
3. Expand:  $HV_{k+p}^+ = V_{k+p}^+ T_{k+p}^+ + f^+ e_{k+p}^T$

## ► Why it works

1. Similar to the implicit QR algorithm for dense eigenvalue problems

$$Q = Q_1 Q_2 \cdots Q_p, \quad H - \mu_i I = Q_i R_i$$

2.  $V_{k+p}^+ e_1 = p(H) V_{k+p} e_1$ , where

$$p(\lambda) = (\lambda - \mu_1)(\lambda - \mu_2) \cdots (\lambda - \mu_p).$$

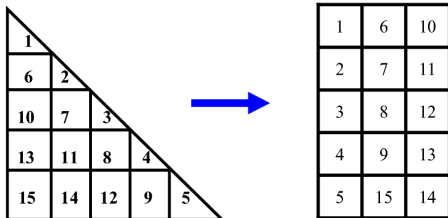
3. Choices of  $k$  and  $p$ :  $k$  number of desired eigenvalues;  $p = k$  or  $p = 20$  (it is the degree of the filtering polynomial)

# Parallelization

- ▶ Source of parallelism
  1. Matrix vector multiplication (MATVEC), application dependant:  $y \leftarrow Hx$
  2. Orthogonalization  $f \leftarrow (I - VV^T)y$
- ▶ Processor to matrix mapping
  - ▶ Hamiltonian: triangular processor grid
  - ▶ Lanczos vectors: remap to a rectangular grid

$d$  **diagonal** processors

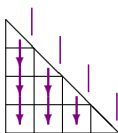
$d(d + 1)/2$  total processors



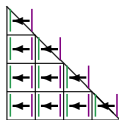
# Parallel Matrix-Vector Multiply

Steps for MATVEC: **input** ( $x$ ) and **output** ( $y$ ) vectors are stored on diagonal processors

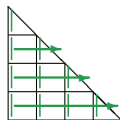
1.



BCast( $x$ )

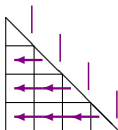


$y \leftarrow Ax$

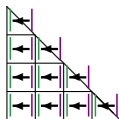


Reduce( $y$ )

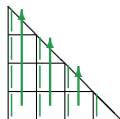
2.



BCast( $x$ )

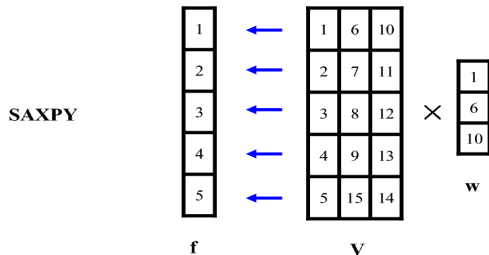
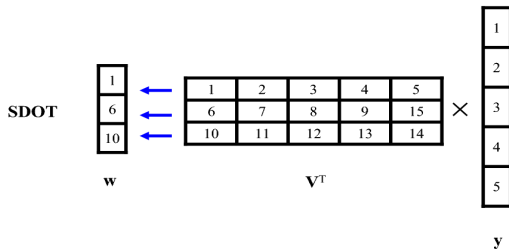


$y \leftarrow A^T x$



Reduce( $y$ )

# Parallel Orthogonalization $f \leftarrow V(V^T y)$

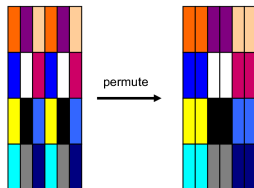


## 2D distributed PARPACK

- ▶ The official release of PARPACK partitions and distributes Lanczos vectors by rows. Orthogonalization becomes costly when `ncpus` is large



- ▶ 2D cyclic distribution



# ARPACK Modification

- ▶ Introduce two additional communicators
  1. All processor group
  2. Row group
  3. Column group
- ▶ Factorization and extend using 2D cyclic distribution along column groups

$$H(V_{k+p}P) = (V_{k+p}P)(P^T T_{k+p})P + fe_{k+p}^T P$$

- ▶ Implicit restart

$$H(V_{k+p}PQ) = (V_{k+p}PQ)[(PQ)^T T_{k+p}(PQ)] + fe_{k+p}^T (PQ)$$

## Performance Improvement for $\text{Li}^6$

Problem size, proc used	1D PARPACK	2D PARPACK
$N_{\max}=6$ , ncpus = 45	211	199
$N_{\max}=8$ , ncpus = 496	342	287



# Conclusions and Future Work

- ▶ Nuclear structure calculation is computationally demanding (large memory usage, irregular sparsity pattern, integer arithmetic);
- ▶ The ordering of MB basis states is crucial for achieving good load balance;
- ▶ Multi-level blocking is essential for efficient Hamiltonian construction; optimal partitions and levels?
- ▶ Alternative Hamiltonian ordering scheme for improving the locality of the data?
- ▶ Explore multi-core architecture to reduce memory usage