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# *Computational Infrastructure for Nuclear Energy Density Functional Theory*

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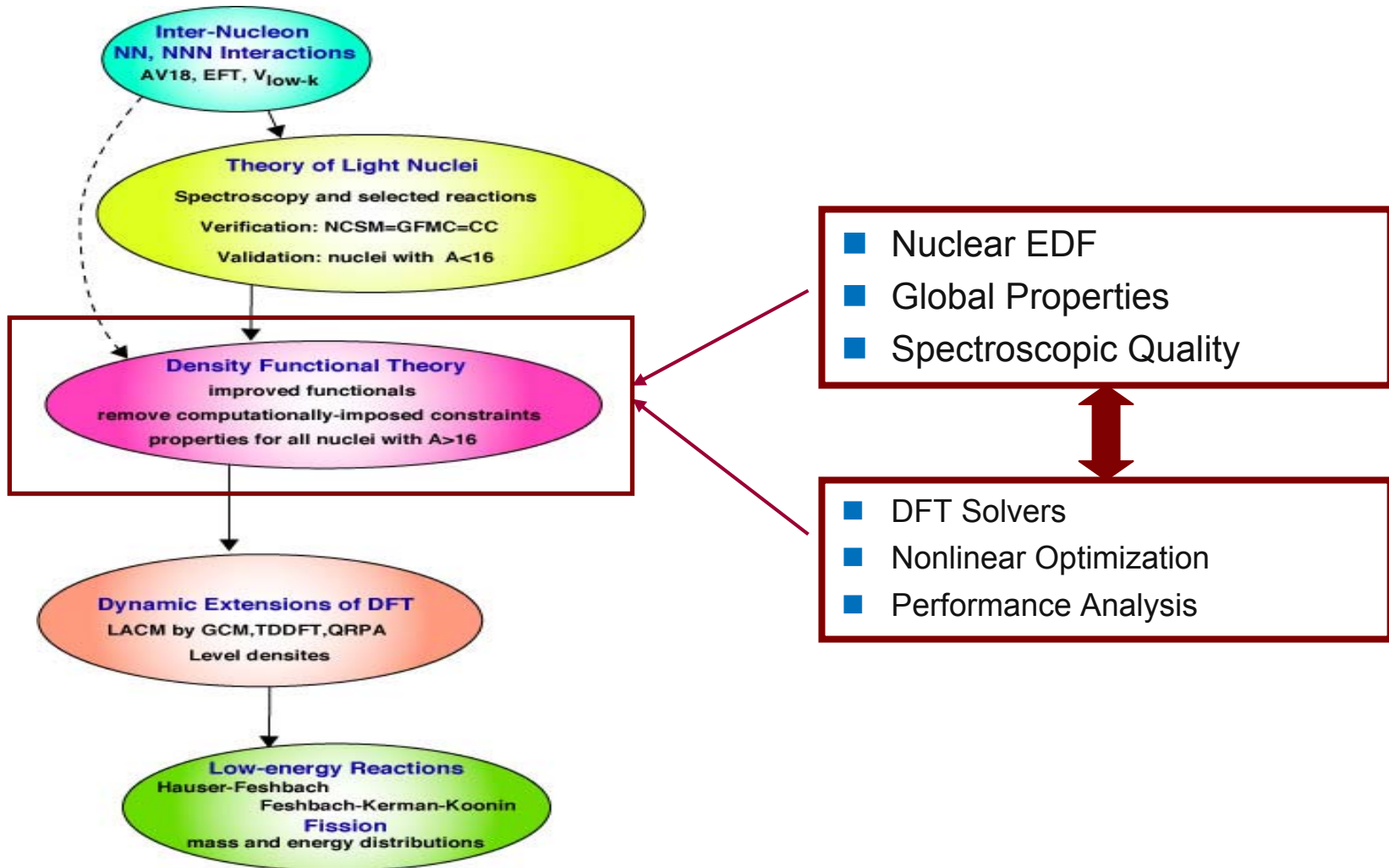
George Fann, Oak Ridge National Laboratory

Jorge Moré, Argonne National Laboratory

April 17, 2008



# The Big Picture



# UNEDF Researchers

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## Nuclear Energy Density Functional Theory

- Witek Nazarewicz
- Mario Stoitsov
- William Shelton
- Jacek Dobaczewski (HFODD)
- Nicolas Schunk (postdoc)
- Carlos Bertulani
- Junchen Pei (postdoc)

## Applied Mathematics Computer Science

- George Fann
- Jorge Moré
- Boyana Norris
- Jason Sarich



# Research Issues: Nonlinear Optimization

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- What are the best techniques for nonlinear, noisy optimization problems

$$\min \{f(x) : x_L \leq x \leq x_U\}$$

when the gradient  $\nabla f$  of  $f$  is not available and the evaluation of  $f$  is computationally intensive (125 CPU days)

- How can we solve systems of  $n$  nonlinear equations

$$H(x) = 0$$

when derivatives are not available and the number of variables  $n$  is large?



# Parameter Estimation in Nuclear Fission: Challenges

The least-squares approach ( ) requires the minimization of

$$f(x) = \sum_{k=1}^m \sigma_k \|f_k(x) - y_k\|^2$$

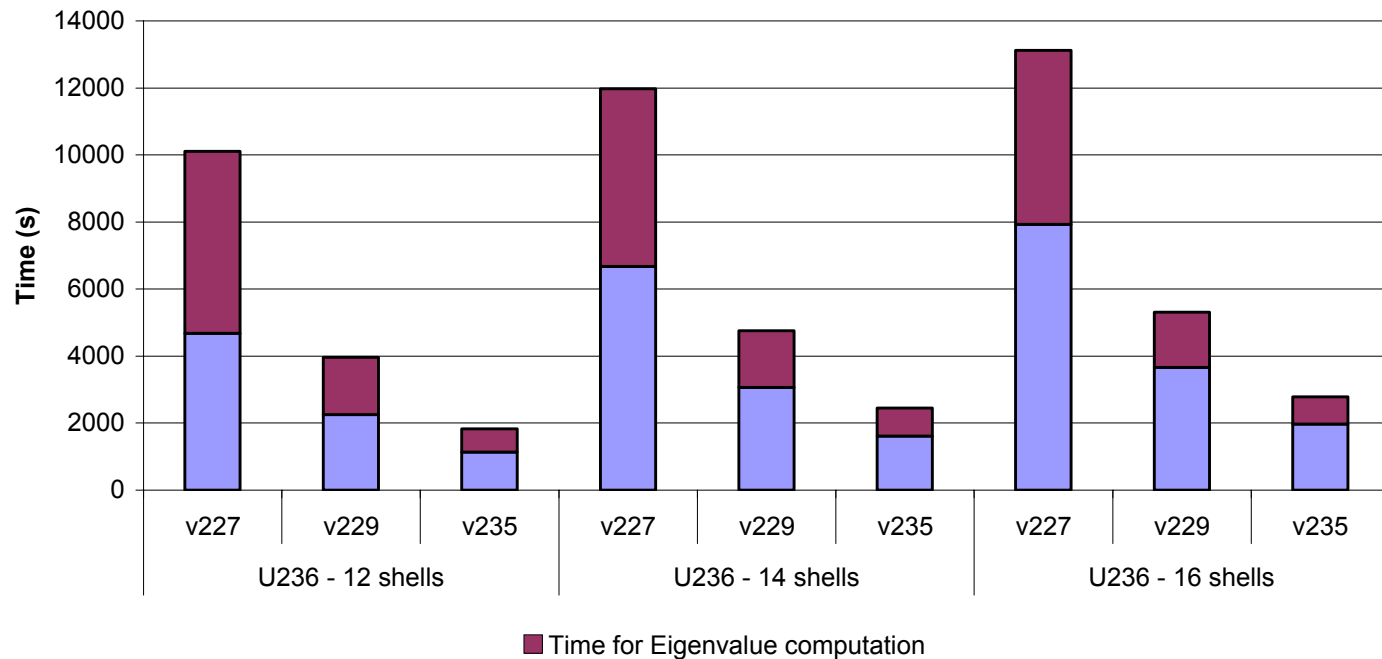
$$x \Rightarrow \text{HFODD} \Rightarrow f_k(x)$$

- Expensive evaluation of  $f_k(x)$  ( $U_{236}$  1.5 hours)
- Large memory requirements ( $U_{236}$  0.5GB)
- Many nuclei (about 2,000)
- A wide range of observables (binding energy,...)
- Noisy function evaluations
- Lack of derivatives with respect to parameters
- Several minima with different predictive powers

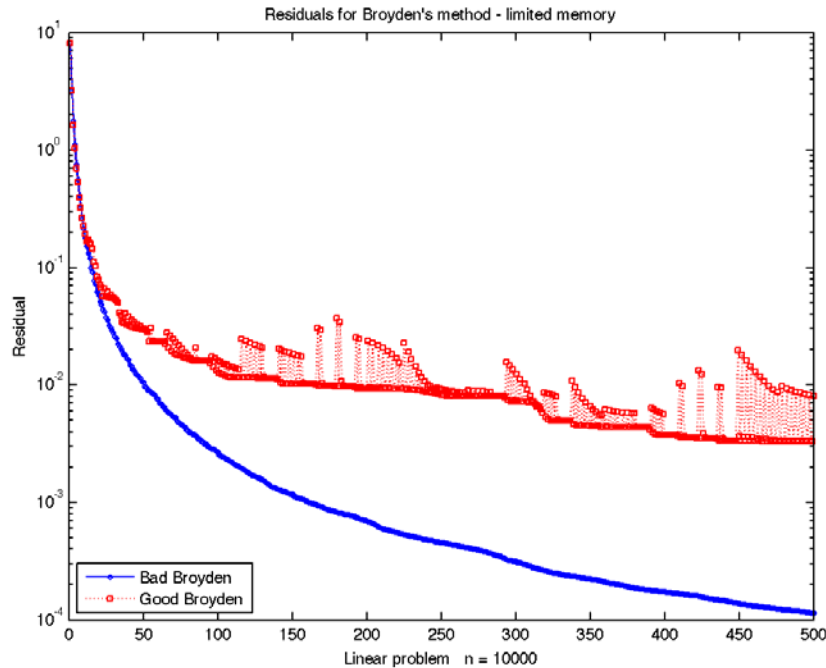


# Performance of HFODD with $U_{236}$

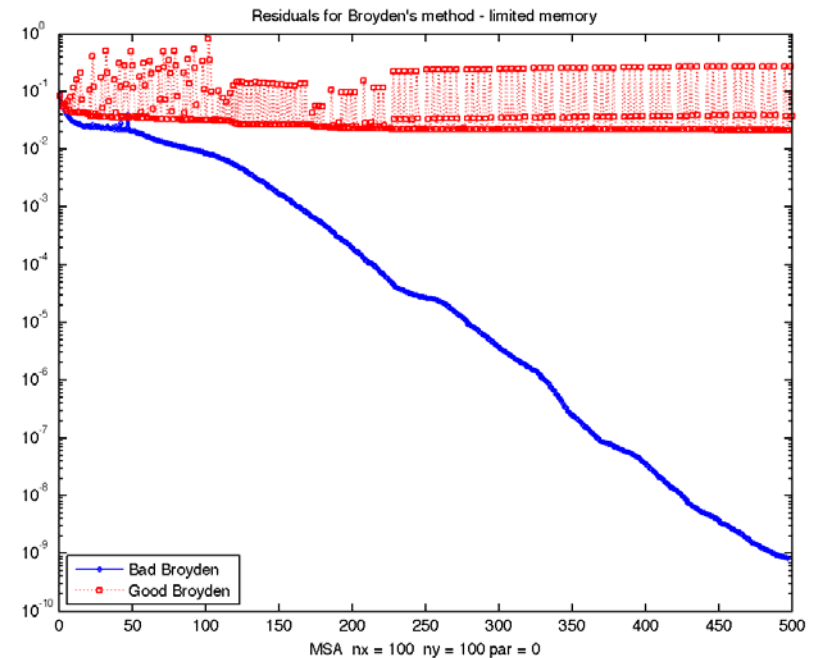
Improvement in computation time for HFODD



# Broyden's Method for Systems of Nonlinear Equations



Linear problem



Nonlinear problem

Compact storage, 10 vector pairs of memory, random starting point



# Contributions: Optimization and Performance Analysis

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- HFODD majordomo list (January 2007)
- Profile of HFODD using Tuning and Analysis Utilities (TAU)
- Introduction of BLAS (40% computing time reduction)
- NEDFT planning meeting (March 2007)
- Full storage eigenvalue solver (60% computing time reduction)
- NEDFT planning workshop (August 2007)
- Analysis of Broyden's method
- Determination of the Nuclear Energy Functional workshop (January 2008)
- *Optimization in SciDAC Applications*, J. of Physics (2007)
- *Benchmarking derivative-free optimization algorithms*, Preprint (2007)





## Future Work

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### ■ Year 2

- Broyden's method for large-scale systems of equations
- Evaluation of Broyden's method in SCF calculations in HFODD

### ■ Year 3

- Development and performance of mass-table algorithms in BG
- Investigation of derivative calculations/sensitivity in HFODD
- Development of model-based derivative-free algorithms

### ■ Year 4

- Model-based and geometry-based optimization algorithms for DFT
- Preliminary investigation of performance on new DFT functionals

### ■ Year 5

- Fission pathways
- Performance, evaluation, and validation of new DFT functional



# Multiwavelets and Fast Methods

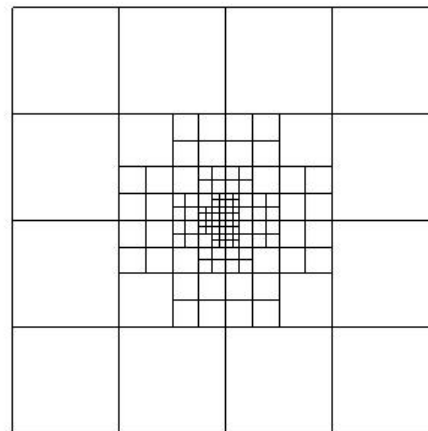
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- Automatic adaptivity for discretization and order of accuracy ( $h$  and  $p$ )
  - Integral and differential operators
  - Functions
  - Compatible between function and operator calculus
- Accurate treatment of singularities
- Accurate treatment of higher order derivatives
  - Improved adaptive treatment of Gibbs type phenomena
- Green's function (Poisson, Helmholtz, etc.)
  - Fast real analysis based  $O(N)$  method
  - Accuracy is proportional to
    - *Degrees of freedom*
    - *Work*
- DFT, Lippmann-Schwinger, Hartree-Fock, ...
- Constructive low separation rank approximation for fast and scalable ( $\log d$ ) methods for high dimensional and non-convolution type kernels



# Multiresolution Methods for DFT

- Adaptive 3-D multiresolution pseudo-spectral methods for nuclei
  - User defined accuracy gives universal reference and good scalability
  - Consistent description of bound and resonant states
    - *Consistent accuracy in neutron-rich or super-heavy nuclei*
    - *Bridge to reaction theory*
- No assumption on symmetry
- Can handle nearly singular or discontinuous functions, and high gradients
- Work is proportional to spectral accuracy
- Controllable and guaranteed precision



Adaptive support of basis functions. A 2-D slice of a 3-D wavefunction from the inverted two-cosh spin-orbit (SO) case

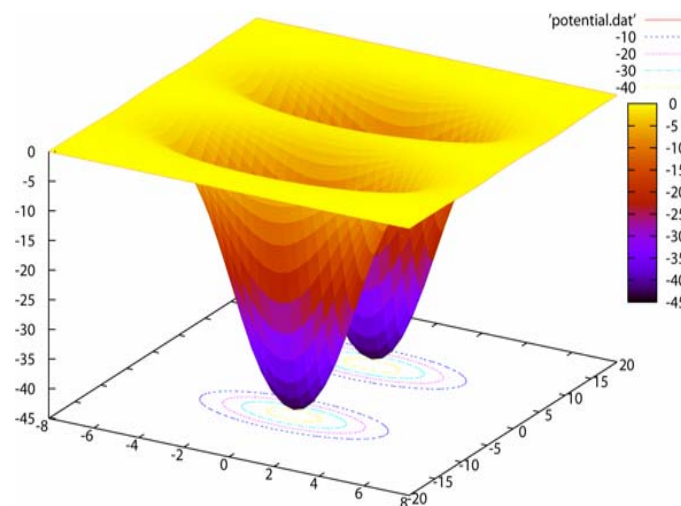


# Contributions: Multiresolution Methods for DFT

- Two-cosh, and PTG are examples of non-localized potentials
- “MADNESS applied to density functional theory in chemistry and nuclear physics,” J. of Physics (2007)
- Benchmarking solvers for nuclear DFT, in progress, preprint (2008), 2 papers in progress
- High accuracy calculations when compared with splines, harmonic oscillators,...(table of comparison, HO, spline, wavelets for 2-cosh, PTG) with and without spin-orbit (C++ version)
- Merging of HO with wavelets for improved starting wavefunctions.
- Parallel C++ code under development, non-spin and spin orbit working...table and preliminary scaling here.

Eigenvalue (exact)	HO Expansion	Multiwavelets $10^{-3}$
-39.7400, $\frac{1}{2}+$	-39.7400	-39.7399
-18.8977, $\frac{1}{2}+$	-18.8977	-18.8976
-0.3205, $\frac{1}{2}+$	-0.1748	-0.3205

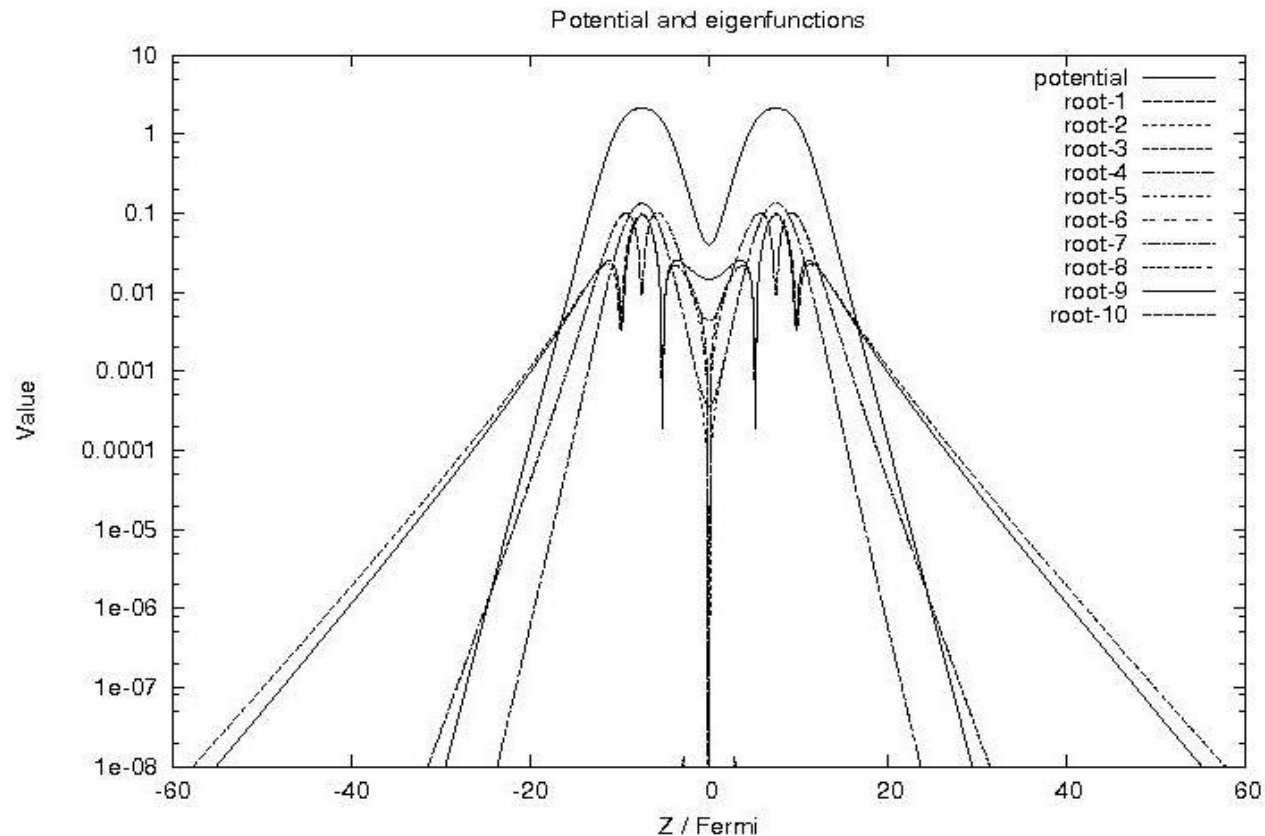
Poschl-Teller-Ginocchio Potential



Inverted 2-cosh (no SO)



# Plot of Potential and Absolute Value of Wave Functions for the 2-cosh Potential



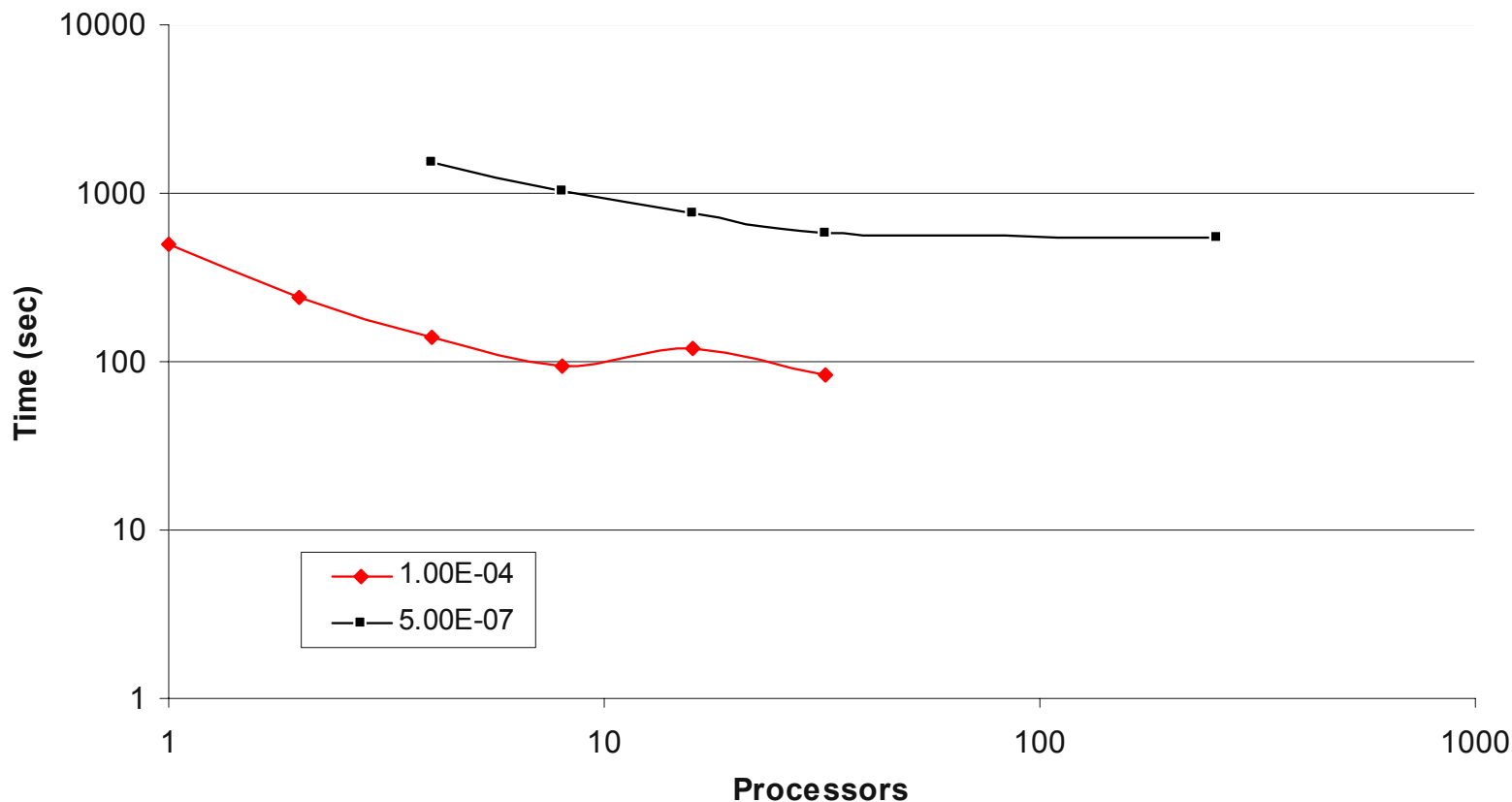
# Results from Harmonic Oscillator, Spline, Multiwavelets and 3D-lattice

Eigenvalue			Inverted 2-cosh potential without spin-orbit				Inverted 2-cosh potential with spin-orbit			
#	Spin	$\pi$	HO, N=22	Spline	Wavelets, 5e-7	3D-lattice	HO, N=22	Spline	Wavelets, 3.e-5	3D-lattice
1	1/2	+	-22.2 <b>3984</b>	-22.24011	-22.24010725	-22.240 <b>20</b>	-22.2 <b>3984</b>	-22.240 <b>0</b>	-22.240107	-22.240 <b>2</b>
2	1/2	-	-22.239 <b>49</b>	-22.23998	-22.23998058	-22.2 <b>4010</b>	-22.239 <b>49</b>	-22.2399	-22.239980	-22.2 <b>401</b>
3	1/2	+	-9.2 <b>1869</b>	-9.22050	-9.22050134	-9.220 <b>62</b>	-9.43 <b>509</b>	-9.436 <b>5</b>	-9.43662	-9.436 <b>74</b>
4	3/2	+	-9.2 <b>0945</b>	-9.21260	-9.21260181	-9.212 <b>71</b>	-9.4 <b>2925</b>	-9.43 <b>19</b>	-9.43202	-9.432 <b>14</b>
5	1/2	+	-9.2 <b>0945</b>	-9.212 <b>47</b>	-9.21260181	-9.212 <b>71</b>	-9.4 <b>2911</b>	-9.43 <b>10</b>	-9.43080	-9.430 <b>92</b>
6	3/2	-	-9.2 <b>0943</b>	-9.21129	-9.21129039	-9.211 <b>40</b>	-9.42 <b>490</b>	-9.4278	-9.42788	-9.427 <b>99</b>
7	1/2	-	-9.2 <b>0943</b>	-9.211 <b>16</b>	-9.21129039	-9.211 <b>40</b>	-8.77 <b>589</b>	-8.7782	-8.77828	-8.778 <b>39</b>
8	1/2	-	-9.2 <b>0269</b>	-9.20595	-9.20595248	-9.20 <b>606</b>	-8.77 <b>013</b>	-8.773 <b>7</b>	-8.77383	-8.773 <b>94</b>
9	1/2	+	-1.7 <b>1590</b>	-1.724 <b>67</b>	-1.72514284	-1.72 <b>840</b>	-1.7 <b>1593</b>	-1.72 <b>39</b>	-1.72516	-1.72 <b>843</b>
10	1/2	-	-1.5 <b>1146</b>	-1.526 <b>21</b>	-1.52690510	-1.52 <b>276</b>	-1.5 <b>1149</b>	-1.52 <b>51</b>	-1.52693	-1.52 <b>279</b>
Moment n=1			20.0	20.0	20.0	20.0	20.0	20.0	20.0	20.0
Moment n=2			0.717832	0.7196883	0.71902147	0.719124	0.7177410	0.719598	0.718931	0.719033
Moment n=3			0.043470	0.043865	0.04379460	0.043805	0.043463	0.043857	0.043786	0.043797



# Parallel Scaling for Nuclear Multiwavelet Code w/o Spin Orbit

## Preliminary Parallel Performance of MADNESS-NDFT on CRAY-XT3



# Future Work

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## ■ Year 2

- Integration of HO with wavelets methods in 3-D
- Testing with other examples
- Conversion to C++ version of the code for MADNESS Nuclear DFT code for parallel computers
- Demonstration for leadership computing platforms
- Solving the symmetry-free non-self-consistent DFT problem
- alpha MADNESS core c++ code at <http://code.google.com/p/m-a-d-n-e-s-s/>

## ■ Year 3

- Development of HF method with realistic effective interactions (Skyrme DFT), Nuclear-MADNESS-HF
- Optimization, code porting and scaling on NLCF machines: Cray and IBM
- Boundary conditions
- Alpha code release of Nuclear physics module using MADNESS

## ■ Year 4-Testing and additions to Nuclear-MADNESS-HFB: Development of version 1.0

## ■ Year 5-Testing of Nuclear-MADNESS-HFB: Application to the fission problem

